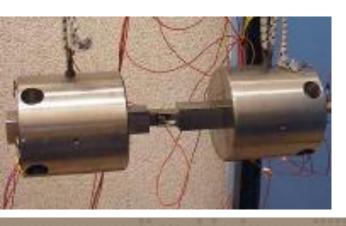
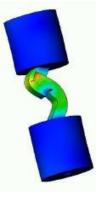


#### Exceptional service in the national interest





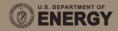






# Project 1: Inverse Methods for Characterization of Contact Areas in Mechanical Systems

Kyle Starkey, Matthew Fronk, Kevin Eschen





#### Introduction



#### Students

- Kyle Starkey (Purdue University)
- Matthew Fronk (Georgia Tech)
- Kevin Eschen (University of Minnesota)



#### Mentors

- Rob Kuether (SNL)
- Adam Brink (SNL)
- Tim Walsh (SNL)
- Matt Brake (Rice University)
- Wilkins Aquino (Duke University)











#### Motivation

#### Interface behavior can effect designs





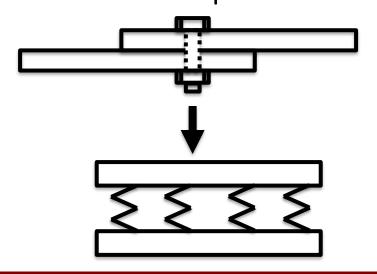


Interfaces are difficult to measure and model

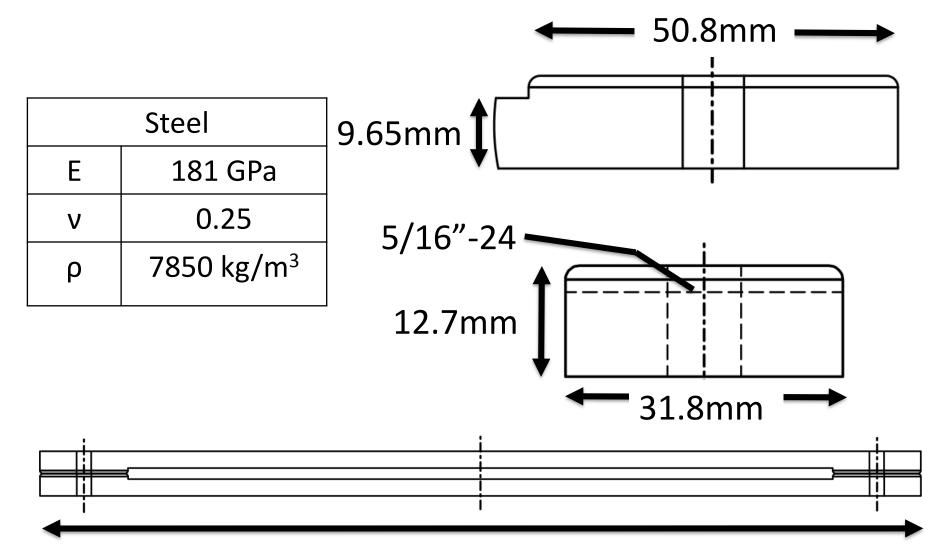


"The Mechanics of Jointed Structures", M. Brake

Simplifying assumptions overlook complex behavior

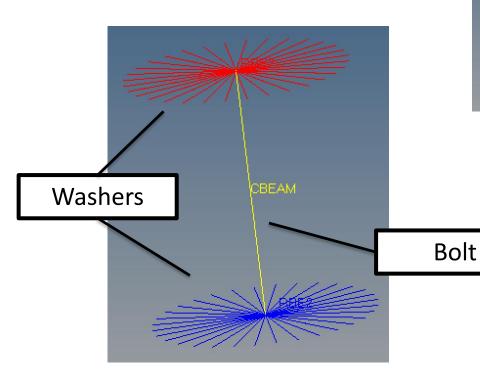


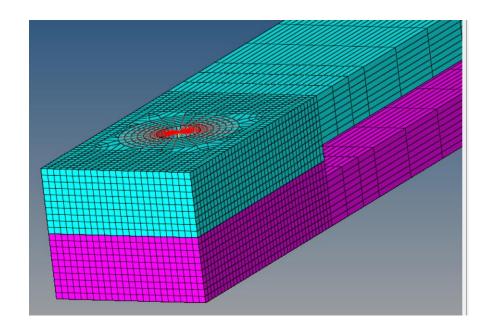
# System



# Static Contact Patch Analysis

- Bolt pretension
- Inertial relief
- Static friction ( $\mu = 0.3$ )
- NL quasi-static solver
- Contact pressure

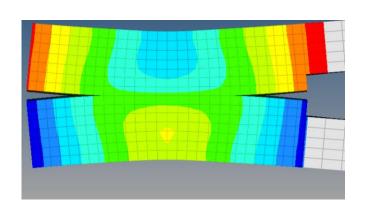


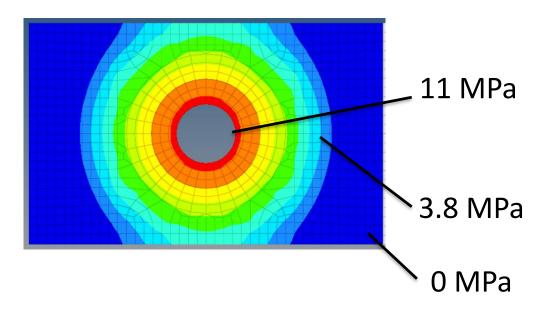


| Torque | Motosh Eqn    | Lacayo et al |
|--------|---------------|--------------|
| Torque | Wiotosii Eqii | Lacayo et ai |
| (N-m)  | Force (N)     | Force (N)    |
| 2.4    | 1685          | 1020         |
| 6.1    | 4276          | 2590         |
| 9.3    | 6479          | 3925         |

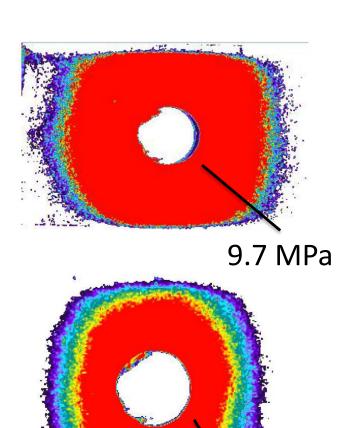
# Static Contact Patch Analysis: Results



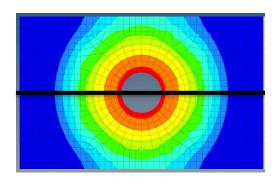


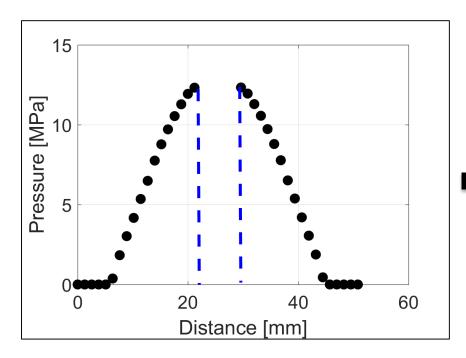


#### Pressure films

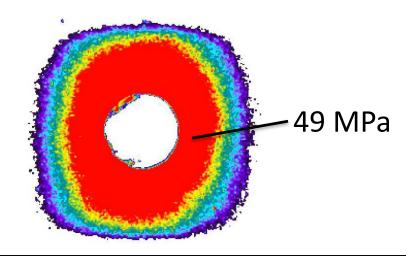


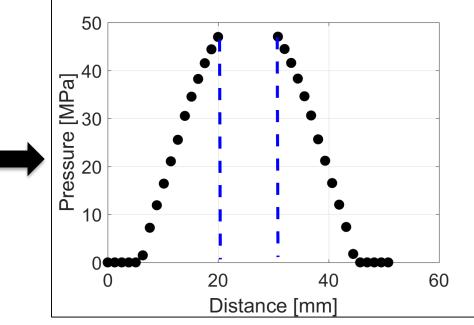
## **Load Calibration**





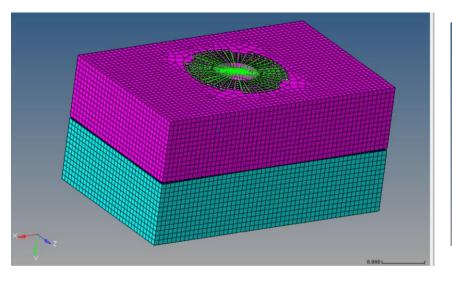
 $F_{preload} = 6479 N \text{ (Motosh)}$ 

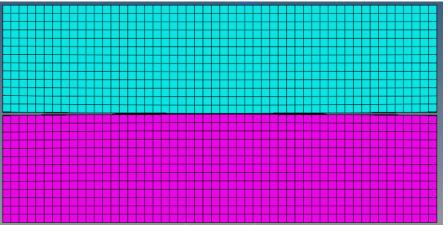


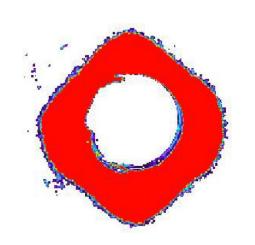


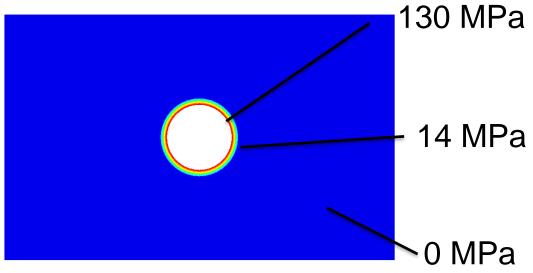
 $F_{preload} = 25500 N$  (Calibrated)

## Rounded Interface





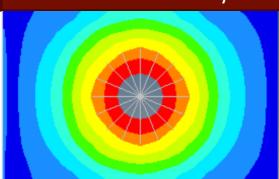




## **SPIC - Definition**

#### Single Parameter Inverse Contact

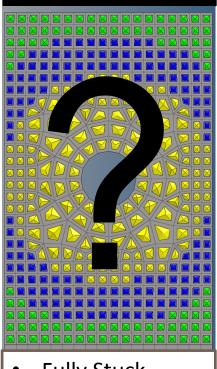
Static Pressure Analysis



#### **System Parameters**

- Geometry
- $E, \nu, \rho$
- $F_{app}$

**Contact Definition** 



- Fully Stuck
- Sliding
- No Contact

Modal Frequencies For multiple elastic

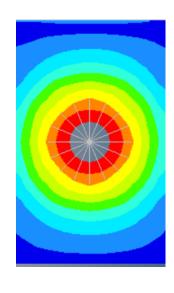
Input

System

Output

modes

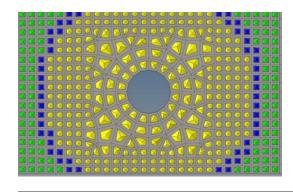
## SPIC – Definition 1

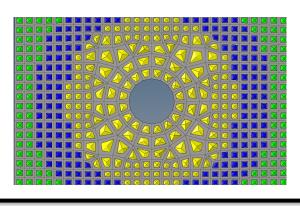


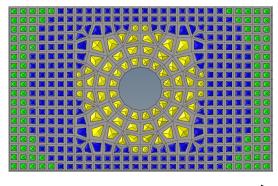
$$0 \ge p_{element} \rightarrow No Contact$$

$$0 < p_{element} < p_l \rightarrow Sliding Contact$$

$$p_{element} \geq p_l \rightarrow \text{Stuck Contact}$$





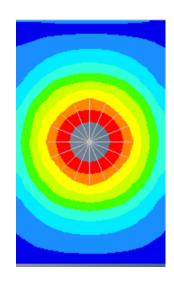


**Mostly Stuck** 

 $p_l$  increasing

**Mostly Sliding** 

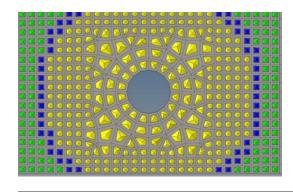
### SPIC – Definition 2

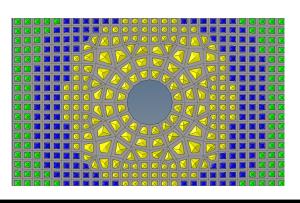


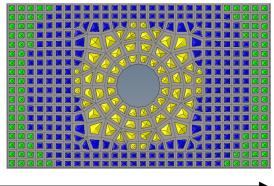
$$0 \ge p_{element} \rightarrow No Contact$$

$$0 < p_{element} < p_l \rightarrow No Contact$$

$$p_{element} \geq p_l \rightarrow \text{Stuck Contact}$$







**Mostly Stuck** 

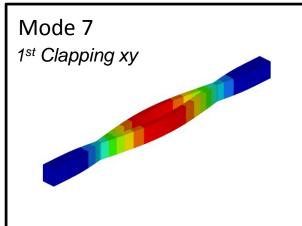
 $p_l$  increasing

Mostly No Contact

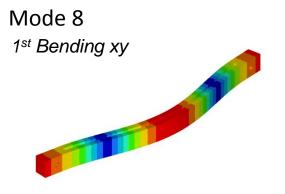
#### SPIC - Goal

Find p<sub>l</sub> at which the numerical simulation matches the experimental modal frequencies

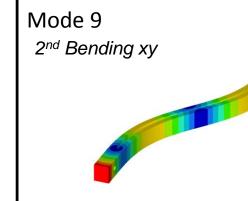
#### SPIC - Modes



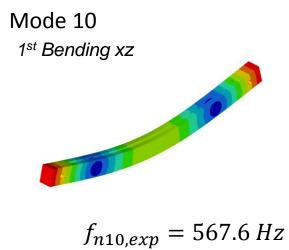
$$f_{n7,exp}=258.0\;Hz$$

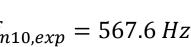


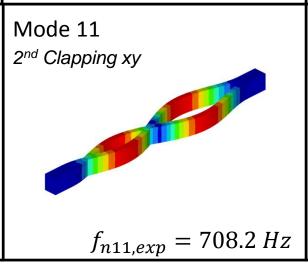
$$f_{n8,exp} = 331.7 \; Hz$$

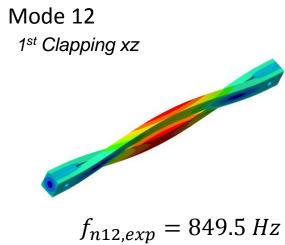


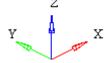
$$f_{n9,exp} = 478.6 \, Hz$$



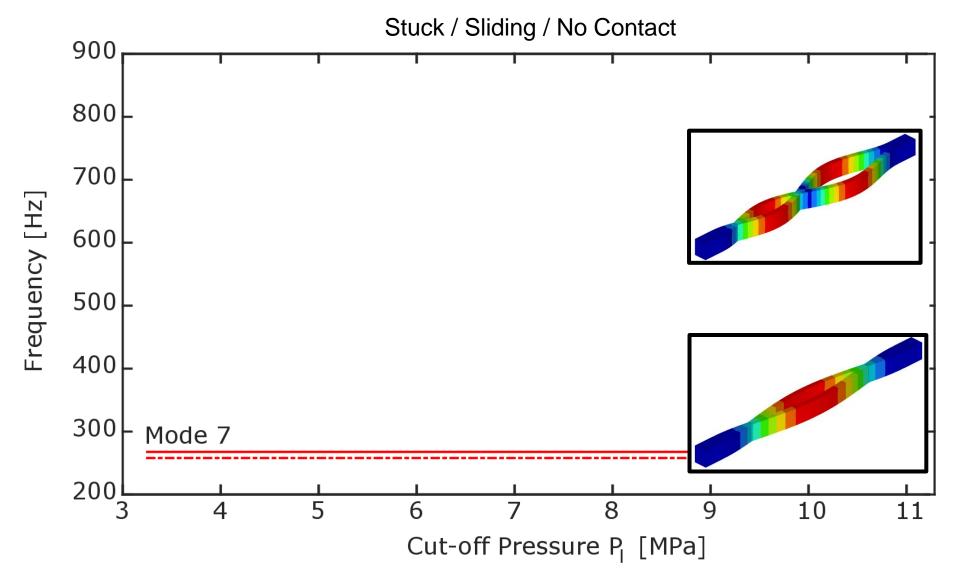




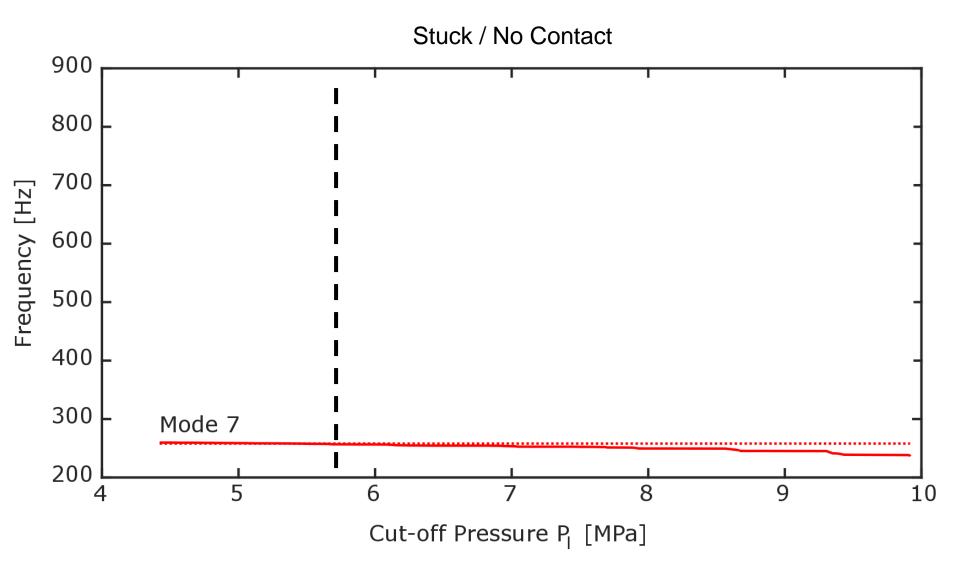




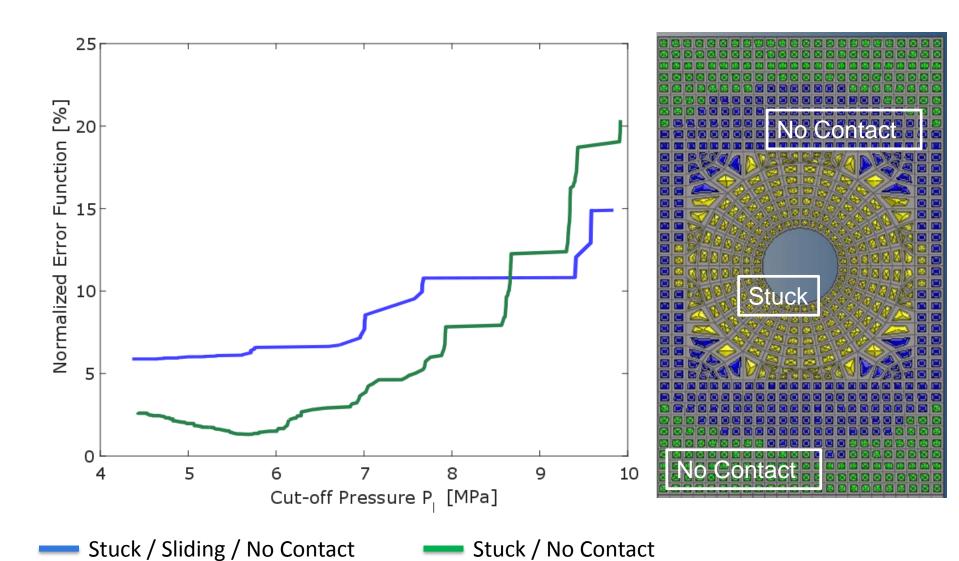
## SPIC-Results 1



### SPIC- Results 2



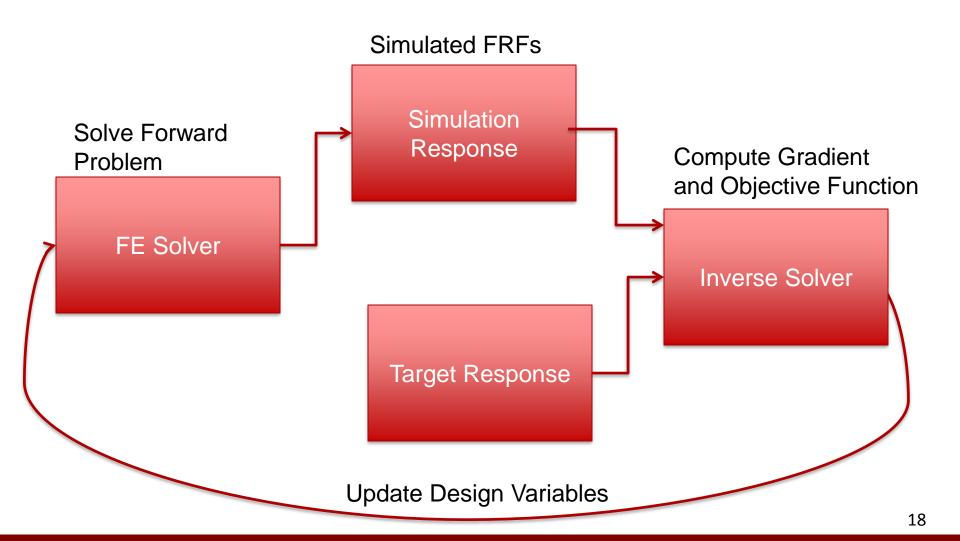
## **SPIC - Results**



#### **Contact Area Inversion**

- Objective: determine contact area from global measurements of displacements
  - We may or may not have a-priori knowledge of contact area, whereas SPIC has knowledge of the static patch.
  - We will represent the contact patch as a density field and enforce contact with a penalty parameter
  - We will only consider stuck contact. So as of now, no friction or sliding contact will be addressed

# Inverse Problems Flow Diagram



#### Forward Problem

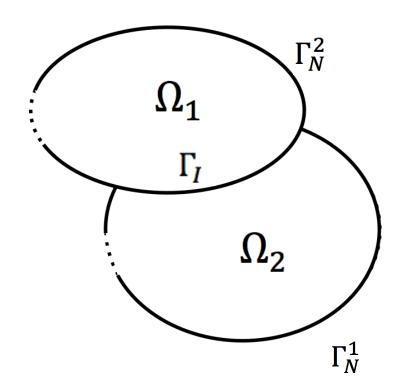
$$\nabla \sigma^{i} + \rho^{i} \omega^{2} u^{i} = 0 \text{ in } \Omega_{i}$$

$$\sigma^{i} n^{i} = \tau^{i} \text{ on } \Gamma_{N}^{i}$$

$$\sigma^{I} n^{I} + \alpha (u^{1} - u^{2}) = 0 \text{ on } \Gamma_{I}$$

$$\sigma^{i} = C^{i} : \epsilon_{u}^{i}$$

$$\epsilon_{u}^{i} = \frac{1}{2} (\nabla u^{i} + (\nabla u^{i})^{T})$$



Where  $\alpha$  is the penalty parameter.

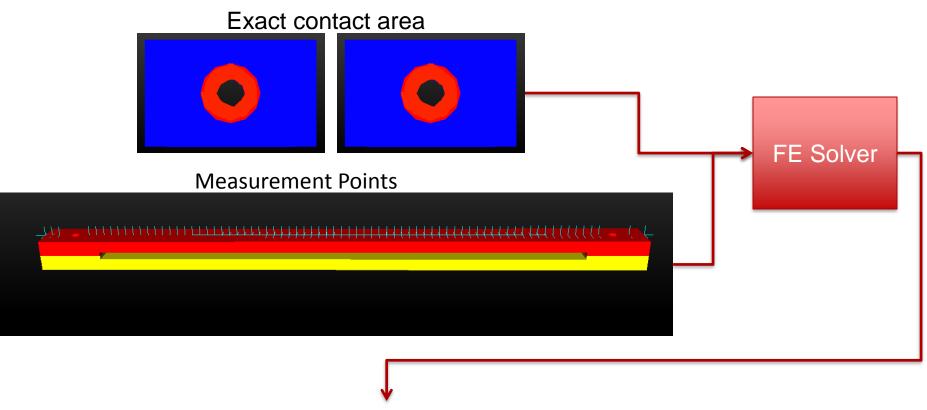
Since we do not know  $\Gamma_I$  beforehand, we will represent it with a density field p.

#### Inverse Problem Statement

minimize  $|(u - u_m)|^2$ where  $u = [u_1, u_2]^T$ subject to:

$$\begin{bmatrix} K_1 - \omega^2 M_1 + \alpha Q_{11}(p) & -\alpha Q_{12}(p) \\ -\alpha Q_{12}(p) & K_2 - \omega^2 M_2 + \alpha Q_{22}(p) \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \begin{bmatrix} F_1 \\ F_2 \end{bmatrix}$$

## Problem Set-up For Numerical Experiment



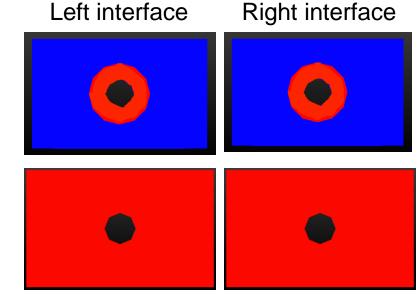
Measured displacement data for the inverse problem!

This is the only knowledge we provide to the inverse method, so we assume no a-priori knowledge of the contact patch profile.

#### **Contact Patch Results**

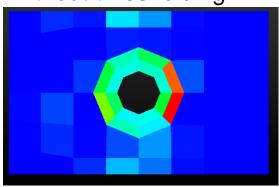
Exact contact area from numerical experiment.

Initial guess: contact everywhere

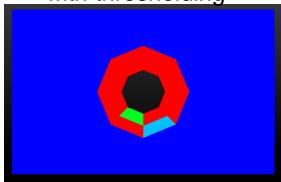


Red: in contact Blue: no contact all other colors are in between

Left interface without thresholding



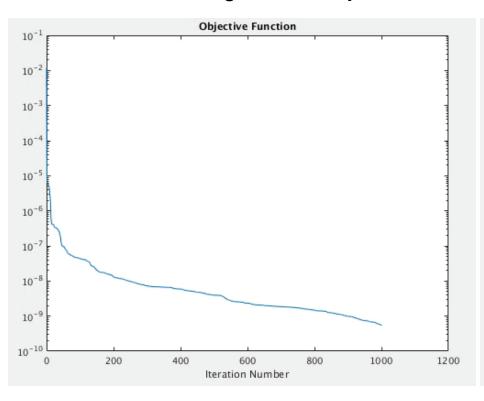
with thresholding

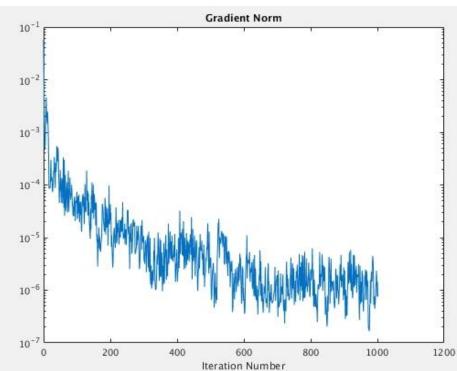


Inverse results: generally finds correct region of contact/no contact

## **Contact Patch Results**

#### Convergence of objective function and gradient during optimization





# Summary and future work

- Preliminary work started with simulated data to understand the problem
- With simulated data, we demonstrated we can obtain reasonable reconstructions of contact area
- It is important to identify the frequencies where there is sensitivity to solution
- Work with experimental data
- Continue to improve formulation by adding a friction model
- Improve numerical performance by adding exact hessian information rather than just using a rank two updates with bfgs.

#### Conclusions

- Static contact patch shapes remain constant for a flat-on-flat interface and can be calibrated to match values of pressure film measurements
- Single parameter inverse contact modeling based on static pressure patches gives physical insight into the contact characteristics of jointed systems

# Acknowledgments

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